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## Location probability distribution of a drifting object

## by Monte Carlo - simulation

Promartec Oy
Erkki Johansson

## ProSAR

ProSAR is C4I decision support system for resource and operation management

- to provide the Maritime Rescue Coordinator, MRC with an intergrated presentation of the data from the different sources
- to carry out the heavy calculations needed in search planning and evaluation
- to provide the MRC with efficient planning tools to optimize the use of the resources
- to provide the MRC with data communication


## OPTIMIZING THE USE OF THE RESOURCES

In case of the search operation, optimizing = maximizing the POS (Probability of Success) of the search tasks


Search object's location probability distribution is needed for POS calculation Location probability distribution can be maintained by the particle based Monte Carlo simulation

## DRIFT CALCULATION BY MONTE CARLO - SIMULATION

-The drift is calculated in a similar manner in the manual method and in Monte Carlosimulation with vector components (sea current, wind current, leeway, tide)
-The trajectory of the drift object is calculated with 15 minutes time step

-Uncertainties of the environmental data (wind speed and direction, current speed and direction etc) are taken into account as drift error factor (normally $=30 \%$ ).
-The radius of the error circle is relative to the distance drifted.

-Uncertainties of the environmental data (wind speed and direction, current speed and direction etc) are defined as standard deviations
-The data is varied during the simulation producing the error vector component.

## LOCATION DISTRIBUTION BY MONTE CARLO - SIMULATION


-5000 or more independent particles, are needed for the position probability distribution
-For the probability map a regular grid is created around all the particles, with desired grid density (default $50 \times 50$ cells).
-POC (Probability of Containment) in each cell is (number of particles within the cell)/( tot.number of particles)
-Probability map is presented as color coded POC- distribution

## PARTICLE PROPAGATION MODEL:

Propagation model defines how the particles reacts on the changes in drifting forces. The random velocity components in the turbulent velocity field (two independent velocity components $u$ and $v$ )


## Random walk

The random walk velocity: for each time step $\mathrm{u}(\mathrm{t})=\sigma \mathrm{Wu}{ }^{\mathrm{n}}[0,1]$ $\mathrm{v}(\mathrm{t})=$ б Wv * $\mathrm{n}[0,1]$ б $\mathrm{Wu*}$ б $\mathrm{Wu}=$ velocity variance ( u ). б $\mathrm{Wv} \mathrm{v}^{*}$ б $\mathrm{Wv}=$ velocity variance ( v ). $\mathrm{n}[0,1]=$ normally distributed random variable with zero mean and variance=1.


## Random flight

The random flight velocity: for each time step $u(t)=A^{*} u(t-d t)+$ б Fu *sqrt( 1-A*A ) *n[0,1]
$A=\exp (-d t / T)$.
$\mathrm{dt}=$ the time step.
$\mathrm{T}=$ the turbulent time scale.
б Fu * б $\mathrm{Fu}=$ random flight velocity variance.


## Ballistic model

The ballistic velocity error:
Constant velocity error
$\mathrm{u}(\mathrm{t})=\mathrm{u}(\mathrm{t}-\mathrm{dt})=\ldots=\mathrm{u}(0)$
$=б \mathrm{Bu}{ }^{*} \mathrm{n}[0,1]$
б $B u^{*}$ б $\mathrm{Bu}=$ velocity variance.

## SCENARIO

A consistent set of fact and assumptions describing what may have happened to survivors. It usually consists of a sequence of actual and assumed events starting sometime prior to the distress incident and continuing to the present time. The most likely scenario(s) is used as a basis for planning searches (IAMSAR 4.6.1)

## POSSIBILITY AREA

The smallest area containing all possible survivor or search object locations. For a scenario, the possibility area is the smallest area containing all possible survivor or search object locations which are consistence with the facts and assumptions used to form the scenario (IAMSAR 4.6.1)

## SCENARIO AND FULL SCALE SITUATION PICTURE



## INITIAL POSSIBILITY AREA <br> INITIAL POSITION PROBABILITY DISTRIBUTION

## ASSUMPTIONS AND UNCERTAINTIES

## vs. POSSIBILITY AREA

- Distress incident position

Affect on initial possibility area

- Distress incident time
- Characteristics of the search object -leeway characteristics
- Environmental data -winds, water currents, waves, temperatures, visibility

Affect on current possibility area

THE BIGGER THE UNCERTAINTIES ARE, THE LARGER IS THE POSSIBILITY AREA

THE MOST COST EFFECTIVE SEARCH IS DONE BY AIMING FOR THE MORE ACCURATE DATA

## INITIAL POSSIBILITY AREA

The smallest area containing all possible survivors or search object locations at the time of the distress incident.

ProSAR supports the followingelementary datum types to define the initial possibility area

- Point datum
- Line datum
- Area datum
- Route datum
- Back Track datum

The initial possibility area can also be defined as a combination of the elementary datums

## INITIAL POSSIBILITY AREA:

## ELEMENTARY DATUM TYPES

## POINT DATUM

- Position (Phi,Lambda)
- Position accuracy
- Normal circular position probability distribution


## LINE DATUM

- Polyline 2...n geographical points in sequence
- Position accuracy
- Normal position probability distribution
 on line cross section



## INITIAL POSSIBILITY AREA:

## ELEMENTARY DATUM TYPES

## ROUTE DATUM

- 2...n waypoints in sequence each point associated with the time.
- Position accuracy
- Normal position probability distribution on line cross section
- Route defined by the user or as known track history of the selected vessel or aircraft


In case distress incident time period the route datum is a part of the route.
In case of exact distress incident time the route datum is a point

## BACKTRACK DATUM

Backtracked
object

Reverse drift calculation for a known object e.g. capsized boat or debris to establish the inital possibility area and position probability distribution of the search object


## INITIAL POSSIBILITY AREA:

 COMBINATION OF ELEMENTARY DATUMS

Any number of different elementary datums (point,line, area, route and backtrack) can be combined to form the initial possibility area

## INITIAL POSSIBILITY AREA: WEIGHTING THE INITIAL POSITION PROBABILITY DISTRIBUTION

- Automatic, time based weighting when distress incident has been defined as time period
- User defined proportional weights for the elementary datums
- User defined hazard areas with desired risk levels


## INITIAL POSSIBILITY AREA:

## USER DEFINED PROPORTIONAL WEIGHTS FOR THE ELEMENTARY DATUMS



## INITIAL POSSIBILITY AREA:

## USER DEFINED HAZARD AREAS WITH DESIRED RISK LEVEL



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## DISTRESS INCIDENT TIME』

## EXACT DISTRESS INCIDENT TIME

-The distress time is known with a high accuracy

## UNCERTAIN DISTRESS INCIDENT TIME

-Distress incident time is not known accurately
-Time is estimated as a time period -The probability of the distress time is evenly distributed within the time period -The uncertainty in the distress incident time increases the possibility area in case of a mobile search object (actively or passively moving seach object)


## DRIFT OBJECT TYPE:

Drift object leeway definitions according to -IAMSAR taxonomy
-US CG taxonomy
-User defined drift object definition


Drift object type uncertainty. Several drift object types for a single search object

## MOBILITY OF THE SEARCH OBJECT

The mobility of the search object after the distress incident
Fixed
-The search object is not moving after the distress incident
Mobile

- Parachute drift, aircraft glide, dead reckoned movement
- Moving actively by own means (walking, swimming, driving a vehicle)
- Moving passively due to the environmental forces (maritime drift)


## MOBILITY OF THE SEARCH OBJECT

PARACHUTE DRIFT, AIRCRAFT GLIDE, DEAD RECKONED MOVEMENT
These movement are taken as an offset to the initial possibility area.


For parachute drift and aircraft glide the high winds has to be defined


## LOCATION PROBABILITY DISTRIBUTION IN THE ARCHIPELAGO



## MULTIPLE SEARCH OBJECTS



The search operation can contain several simultaneous search objects

## 'PREVIOUS SEARCH - EFFECTS' ON POSITION PROBABILITY DISTRIBUTION



Scatter dots are color coded according to the current POE (particle's Probability Of Existence)


## PROBABILITY MAP AND 3D-DISTRIBUTION



After the search


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## The End

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